

# Real-time Avoidance Strategy of Dynamic Obstacles via Half Model-free Detection and Tracking with 2D Lidar for Mobile Robots

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**Abstract**—Avoidance is a necessary capability for a mobile robot to perform tasks such as delivering obstacles in household or industrial scenarios. The existing avoidance strategy based on TEB (Timed Elastic Band) local planner and cost-map provided by Robotics Operating System(ROS) cannot realize the excellent performance when a robot and an obstacle both move. In this work, we present a real-time, simple and reliable approach to detecting and tracking obstacles via a two-dimensional (2D) lidar in dynamic scenarios where the mobile robot and the obstacle are moving. Obstacles are represented by a set of points against their outlines and the information of obstacles is initialized and updated via the raw laser measurement. First, the obstacle is detected by three main steps: pre-processing, segmentation and merging, classification of consequent measurements. Second, we use a hierarchical method to realize data associations for figuring out the corresponding matches among obstacles with the consecutive time. Last, after doing the data association, we need to estimate the motion of the dynamic obstacle for being tracked by the Kalman filter. Extensive experiments performed in the simulation and practical scenarios indicate that the proposed method enables a mobile robot to perform dynamic avoidances efficiently. An additional video is attached to this work in YouTube, <https://www.youtube.com/watch?v=A2Ad8rNqQYw>.

**Keywords**- Obstacle detection; Obstacle tracking; Dynamic avoidance; 2D lidar; Mobile robot

## I. INTRODUCTION

AVOIDING obstacles, a key function of mobile navigation, poses a typical challenge for mobile robots, for which the real-time perception is considered as the key bottleneck because there is a large amount of the environment information that needs to be processed. The detection and tracking of participants such as pedestrians and robots play a crucial role in a safe mobile navigation. A common scenario involves the autonomous navigation of a mobile robot, in which a robot is required to detect obstacles and predict the motion of moving obstacles in unstructured environments, as

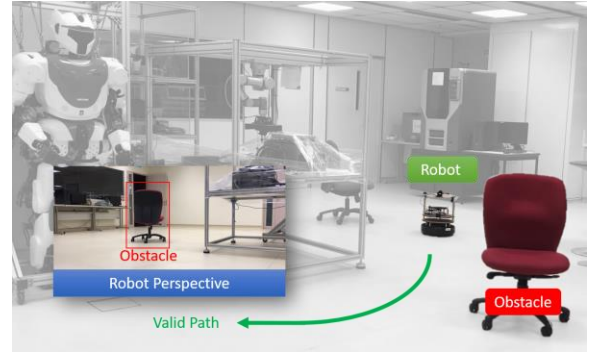


Figure 1. Robot avoiding an obstacle based on the proposed algorithm.

shown in Fig. 1. The perception efficiency for dynamic avoidance yields the limitations of the capability of robots making decisions such as avoidance actions, especially in typical human-involved environments with considerable clutter. Moreover, few of the perception strategies can run in real time due to a large number of relevant vectors.

In terms of robotic applications, a perception system interprets the surroundings using visual cameras and/or laser scanners[1-6]. Although vision-based perception approaches have advantages especially in semantic understanding[7], their major limitations result in high sensitivity to illumination. Here we consider the 2D point-cloud measurement from a 2D lidar which is with high resolution, insensitive to lighting conditions, and just costs less computational resource. There is a classical avoidance strategy including the timed elastic band (TEB) local planner[8-10] and the cost-map converter in ROS[11]. Specifically, the TEB problem is formulated as a weighted multi-objective optimization framework by dynamic constraints of the motions. Moreover, the TEB local planner utilizes a cost-map converter [8-10] to transform occupied cells of 2D map to a set of convex geometric primitives (points, lines, polygons) that represent obstacles in the map by clustering. By integrating the geometric primitives representing obstacles during the navigation period, the TEB local planner can avoid obstacles. However, all the obstacles detected by a mobile robot are also divided into a large number of geometric primitives considered as obstacles by TEB local planners, which lead to a considerable computational resource. Thus, a mobile robot with the TEB local planner has unsatisfactory performances in avoiding dynamic obstacles.

The target of this work is to achieve safe navigation for a mobile robot in indoor environments with some pedestrians. We propose a principled framework for the detection and tracking of dynamic obstacles by means of one single 2D lidar

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regardless of obstacle classes and shapes, integrating the TEB local planner to realize obstacle avoidance. The circles with infinite height and the line are used to be representatives for modeling the obstacles in the environment. To realize a collision-free navigation, we approximate the real underlying model of the obstacle which is deemed acceptable for yielding a dynamic local map since the obstacle recognition is not our objective. The motivation of the line and the circle representing obstacle models is threefold. Firstly, a large obstacle such as a long wall is represented by a line with just two endpoints. Secondly, smaller obstacles such as desk legs or moving persons in practical scenarios are in general modeled as cylinder-like shapes. Thirdly, the circle model with three parameters in the 2D space is inexpensive to compute comparing to occupancy grids. Thirdly, enlarging the dimension of the cylinder can generate a safe distance between an obstacle and a moveable robot. As for the pre-processing, we first use the median filter to discard the noise and segment the 2D point cloud into independent laser-point cloud blocks collected by the 2D laser. Then, using geometric primitive representation, the segmentation is performed on laser-point cloud blocks, followed by merging (clustering) laser-point cloud blocks with small distances. Further, all the detected obstacles are modeled as lines and circles. Despite a higher computation resource, we indicate that some online calculations can still be completed. Finally, we utilize a hierarchical data association strategy based on Kalman Filter (KF) to estimate the motions.

We aim to achieve a better avoidance strategy by the proposed obstacle detection and tracking algorithm when the mobile robot and the obstacle are moving. However, the robotic navigation is a systemic work, not only combining the perception system but also integrating the robotic control[12], planners[13] and localization[14]. In this work, the simple designed controller based on a differential kinematic model is used for driving a two-wheel mobile robot. The global planner in ROS is integrated into the robotic navigation system for planning a global path and a particle filter-based adaptive Monte Carlo localization (AMCL) is adopted for tracking the robot's pose in a known map extracted from 2D data.

We organize the paper as follows. After reviewing existing methods in section II, we introduce the core concept of detecting and tracking dynamic obstacles in detail in section III. The performance of the proposed avoidance strategy is evaluated by abundant experiments in section IV. Finally, the conclusion is made in section V.

## II. RELATED WORK

There exists a vast amount of research works regarding the problem of detection and tracking of multiple dynamic obstacles.

In terms of describing the surrounding environment, these existing lidar-based approaches can mainly be classified into two categories in detail: 1) grid-based [15, 16] and 2) vector-based [3] methods. Most of approaches apply the 2D or 3-dimensional(3D) occupancy grid (grid-based) to represent environments [17]. In particular, the occupancy grid in a map is divided into spaced cells and then complex geometries are used for representing obstacles for detecting and tracking obstacles. For example, the grid trajectories features were

applied to detecting dynamic obstacles in [18]. Another commonly used representation of the environment, the vector-based method, incorporates simple and higher-level predefined geometric features such as line segments, circles, ellipses and rectangles, boxes to directly model obstacles in[19-21]. Therefore, obstacles described by geometric features can be expressed via the pose(position and orientation) of the geometric feature. In comparison to the first category, the vector-based approach with the compact representation of the surrounding environment is particularly suitable for describing a sparse scenario due to the low memory consumption. Our work concentrates on the obstacle detection and tracking by 2D vector-based representatives.

The dynamic obstacle avoidance system involved by the perception prediction and path planning is modifying and estimating the pose of a moving robot in real time such that the robot is able to avoid collisions with moving obstacles found on its path. There are several classical methods such as virtual force field(VFF) [22, 23], vector field histogram(VFH) [24], dynamic window approach(DWA) [25]and TEB approaches[8, 9, 26]. In terms of VFF [22, 23], the histogram grids are applied to representing the area through which the robot can pass. However, such a method is not available when the mobile robot and moving obstacle close to each other generate the repellent effect. To address such an issue in VFF, Borenstein et al.[24] presented the VFH method that employs the 2D histogram grid to describe the surroundings for obtaining a one-dimensional polar histogram constructed around the momentary location of the robot. In contrast to VFF and VFH methods, DWA was developed to avoid obstacles by means of defined cost functions based on the constraints of mobile robots [25] on the kinematics and dynamics. The elastic band based method can adapt to dynamic path changes by adjusting the path to generate a new one once a new obstacle is detected [26].

## III. METHODOLOGY

In the section, we first introduce how to detect obstacles (A). Then, the details of tracking obstacles are described (B).

### A. Obstacle Detection

#### 1) Pre-processing

A set  $\mathbf{p}$  with  $N$  measurement points is from a lidar scan. We represent each raw point  $p_i$  in  $\mathbf{p}$  in the form of Polar coordinates  $(R_i, \theta_i)$  as follows,

$$\mathbf{p} \triangleq \{p_i = (R_i, \theta_i)\}, i \in [1, N] \quad (1)$$

The accuracy of measurements is disturbed by the noise. The outliers may lead to such a situation where some measurement points fail to represent an obstacle as they may be unstable or noise points in practical environments. A range filter is integrated into the proposed algorithm to remove useless points with invalid values represented by NaN or beyond the range. A  $3 \times 3$  median filtering matrix is applied to smoothing the 2D point data. The distance of a point  $i$  from a laser scan as  $R_{(t,i)}$  at the current time  $t$ . Thus, the  $3 \times 3$  median matrix used for filtering out some points is given as follows:

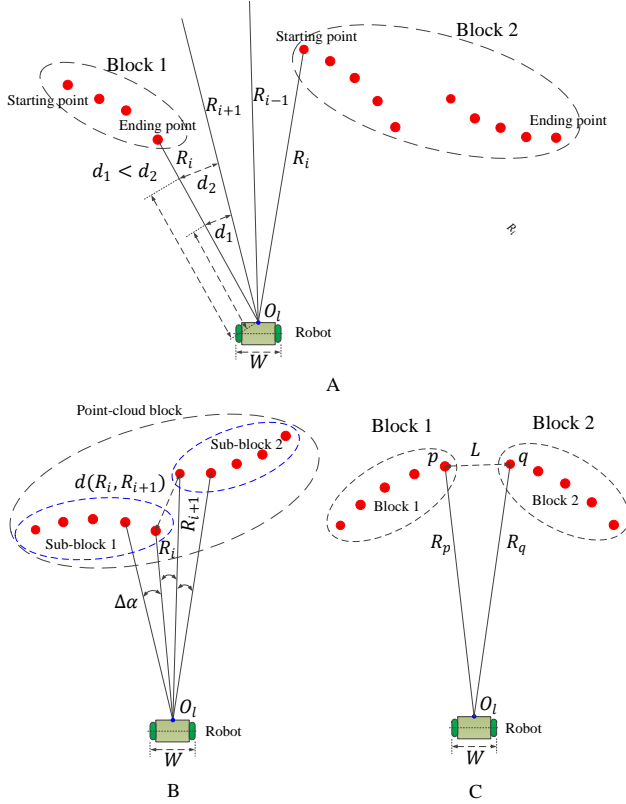


Figure 2. Segmenting the laser-point cloud into independent laser-point cloud blocks(A), segmenting one block into two small blocks (B) and merging two blocks into one blocks(C).  $d_1$  or  $d_2$  is the different of two points, on the two laser rays, with equal distance to the laser origin  $O_i$ ;  $R_i$  represents the distance of the point  $i$ ;  $d(R_i, R_{i+1})$  denotes the distance the two sequential measurement points;  $L$  indicates the distance between the termination points of two adjacent laser-point cloud blocks;  $W$  represents the width of the robot; the red dots are the laser points.

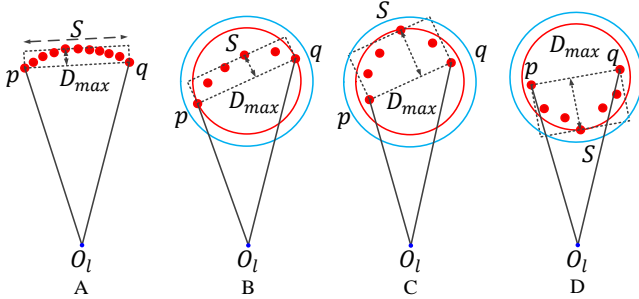


Figure 3. Classification of segments. The two points with the starting index  $p$  and the ending index  $q$  in a laser-point cloud block;  $S$  denotes the distance between  $p$  and  $q$ ;  $D_{max}$  represents the maximum one among distances from points on the laser-point block to the line segment formed by  $p$  and  $q$ ;  $O_l$  is the laser origin; the dashed rectangles cover all the laser points and the red dots are the laser points.

$$\begin{bmatrix} R_{(t-1,i-1)} & R_{(t-1,i)} & R_{(t-1,i+1)} \\ R_{(t,i-1)} & R_{(t,i)} & R_{(t,i+1)} \\ R_{(t+1,i-1)} & R_{(t+1,i)} & R_{(t+1,i+1)} \end{bmatrix} \quad (2)$$

We use the median of the 9 elements in the median filter as the distance between the laser point  $i$  and the laser mounted on the robot at the time  $t$  for discarding noise points in consideration of the space and time, reducing the complexity and increase accuracy of the obstacle classification.

After filtering out the noise points, we segment a large laser-

point cloud into independent small laser-point cloud blocks in order. For each laser-point cloud block, the starting point index satisfies  $R_{i-1} = 0$  and  $R_i \neq 0$ . Moreover, the ending point index satisfies  $R_i \neq 0$  and  $R_{i+1} = 0$ , as shown in Fig. 2(A).

## 2) Segmentation and merging

All laser points are segmented into point-cloud blocks that have strong correlations based on practical properties. There exist two main segmentation types for the point cloud measured via a lidar such as the complete segmentation and the partial segmentation. The complete segmentation means one obstacle is considered as one single segment. In terms of the partial segmentation, one obstacle can be characterized by two or more segments (e.g. human legs). In this work, we work on the partial segmentation. In practical environments, some large segments, such as walls, are usually interrupted by small intervals, which results in a wrong case that one obstacle is represented by more than one segment. It is obvious that the density of measurements gradually decreases in the lidar data and the layout of points becomes sparse as the measured distance increases (see Fig.2-A). Here we use the distance of two endpoints of the small interval to determine the segmentation.

For segmenting the data after filtering, we first determine the distance  $d$  between the two sequential measurement points  $i$  and  $i + 1$  defined in the polar coordinate.

$$d(R_i, R_{i+1}) = \sqrt{R_i^2 + R_{i+1}^2 - 2R_iR_{i+1} \cos \Delta\alpha} \quad (3)$$

where  $R_i$  and  $R_{i+1}$  represent the measurement distances of the points  $i$  and  $i + 1$ .  $\Delta\alpha$  denotes the resolution angle of the lidar. If  $d$  is bigger than  $kW$ , the laser-point cloud block is segmented into two small blocks, as shown in Fig.2(B).  $W$  denotes the width of the robot and  $k$  is the setting dynamic amplification factor as follows

$$\begin{cases} k = \frac{W \cdot R_i \cdot R_{i+1}}{100(R_i + R_{i+1})}, & \frac{R_i + R_{i+1}}{2} > T_d; \\ k = 0.15, & 0 < \frac{R_i + R_{i+1}}{2} \leq T_d. \end{cases} \quad (4)$$

where  $T_d$  ( $T_d=10$ ) is a threshold of the measured distance. We define the dynamic amplification factor  $k$  to adjust the distance threshold between the two adjacent points with the width of the robot and the measured distance changing. For example, as the measured distance increases, the distance between two adjacent lidar points also becomes larger. We increase the threshold to reduce the number of segments. Moreover, if the robot width is large, the small gap with a small distance between the two adjacent points tends to merge together so that the robot cannot go through the gap and reduce the number of segments in the long distance.

The merging processing needs to be done for some laser-point cloud blocks. As shown in Fig. 2(C),  $L$  is the space distance between the termination point of the first point set with the index value  $p$  and the starting point of the last point set with the index  $q$ . This connection can be done if the following condition is met. The robot cannot pass the narrow gap if  $L$  is smaller than  $W$ :  $L < W$ . The enhancement of the algorithm involves the combination of two segments separated by a small interval. In this case, these two laser-point cloud blocks are merged into one laser-point cloud block, as shown

**Algorithm 1:** Splitting segments into subsets**Data:**

$N \leftarrow$  The number of measurement points in the point-cloud block  
 $B \triangleq \{p_i\}, i \in [1, N]$ ;  
 $T_n \leftarrow$  The threshold;  
 $D_m \leftarrow$  The maximum value of the distances between each point and the line fit by two endpoints;  
 $S \leftarrow$  the distance between two endpoints;  
 $V_{result} \leftarrow$  the vector storing the point-cloud block with  $N$  less than  $T_n$ ;  
 $V_c \leftarrow$  the vector storing the point-cloud block with  $N$  more than  $T_n$ ;  
 $N_c \leftarrow$  the number of elements in  $V_c$ ;  
 $N_{c0} \leftarrow$  the number of points in  $V_c[0]$ ;

```

Put B into Vc
1 While (Nc0 ≠ 0) do
2   If (Nc0 > Tn)
3     Calculate Dm of Vc[0] and get pk that corresponds to Dm
4     If (Dmax > 0.2|S|)
5       Split Vc[0] into B1 (B1 ≜ {p1, p2, ..., pk})
        and B2 (B2 ≜ {pk, pk+1, ..., pNc0})
6       If (k > Tn)
7         Put B1 into Vc
8       Else
9         Put B1 into Vresult
10      If (n - k + 1 > Tn)
11        Put B2 into Vc
12      Else
13        Put B2 into Vresult
14      Delete Vc[0]
15    Else
16      Delete Vc[0]
17  Else
18    Delete Vc[0] in Vc
19    Put Vc[0] into Vresult
20 End
Output: Vresult

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in Fig.2(C). Also, we compensate the corresponding values to those laser points between  $p$  and  $q$  for making the two combined point sets spatially continuous. In order to determine the number  $N$  of the compensated points, we calculate the average distance  $d_{aver}$  of the adjacent points of two point-cloud blocks and then,  $N = \frac{L}{d_{aver}}$ . The distances of 2D points  $p$  and  $q$  is  $R_p$  and  $R_q$  respectively, thus the distance of the compensated point  $i$  is represented as follows,

$$R_i = R_p + i \cdot \frac{R_q - R_p}{N}. \quad (5)$$

### 3) Classification

By segmenting and merging, the point cloud coming from a laser consists of independent point sets (point-cloud blocks). The basic idea of classification is to describe any obstacle via a set of simple shapes[27]. The point-cloud block can be formulated as two basic shapes such as the circle, liner segment. The approximation of the point-cloud blocks based on these geometric models has two major advantages. First, a number of discrete points used for representing any obstacle are replaced by just inexpensive parameters such as position and radius, which simplifies computing. Second, such averaging effect for describing the model can be robust to cope with the measurement noise. Although such an approximation may result in unnecessary loss of motion space of the mobile robot. Indeed, as our main target is to realize a safe dynamic navigation rather than the obstacle recognition, the real

underlying model of the obstacle can be approximated is deemed acceptable.

To store the obstacles for further processing, we build a set of obstacles as  $\mathbb{O}$ ,  $\mathbb{O} \triangleq \{\mathbb{L}, \mathbb{C}\}$ .  $\mathbb{L}$  denotes a set of line-type obstacles and  $\mathbb{C}$  represents a set of circle-type obstacles.

(1) If the number of points of a point set is more than a predefined threshold  $T_n$  ( $T_n = 10$ ), we first use a line segment to connect the starting point  $p$  and the ending point  $q$  and then, calculate the maximum value  $D_{max}$  of distances from each point to the line segment, as illustrated in Fig. 3. If  $D_{max} < 0.2|S|$ , this point-cloud block will be fit to a line segment with two endpoints  $p$  and  $q$  (see Fig.3-A).

If  $D_{max} > 0.2|S|$ , the point-cloud block can be split further. The corresponding algorithm is shown in Algorithm 1. We recursively repeat this procedure for each new subset. When the number of points in a new subset is less than  $T_n$ , the splitting stops.

(2) When the number of points in the point-cloud block is less than  $T_n$ , we utilize a circle to represent this point-cloud block with a relatively small size. There are two main reasons. First, if the size of point-cloud segments is very large (e.g. corridor walls), the circle extracted from such a segment would cause that an obstacle covers a vast area of the workspace. The circle representative is suitable for a point-cloud block with a small size. Second, indeed, the size of a dynamic obstacle (e.g., humans) is far less than that of static obstacles (e.g., walls) in indoor environments.

To determine the radius of the circle extracted from a point-cloud block, we first use the method stated above to fit the point set. When the point-cloud block satisfies  $D_{max} < 0.2|S|$ , the midpoint of line segment connected by two endpoints is set as the center and the distance between the center and the maximum-distance point is the circle's radius (see Fig.3-B). Otherwise, we first need to determine the convexity or concavity of the point-cloud block since the parameters of the circle extracted from a point-cloud block depend on the convexity or concavity.

Here we propose a highly efficient algorithm to determine the convexity or concavity of the point-cloud blocks based on the vector cross product, as shown in Algorithm 2. We first take the two endpoints of the segment and then, obtain the midpoint of them, considering the midpoint as the center of the estimated shape. Further, the distance from the center to each point of the segment is calculated so that the maximum one among these distances is extracted. Lastly, this maximum distance serves as the circle's radius.

In order to realize a free collision between a robot and an obstacle, the radius of the circle is enlarged by a margin value defined as a safe distance, as shown in Fig.3(blue circles). If this segment is concave, the zone of the triangle formed by two endpoints of the segment and the origin of the lidar is free for the mobile robot (Fig.3-C). While if the segment is convex, the zone between the origin of lidar and the nearest point from the lidar to the segment is safe. The robot can move at the safe zone (Fig.3-D). All the point-cloud blocks represented by circles are added to the set  $\mathbb{C}$ .

### B. Obstacle Tracking

We implement a simple Kalman filter[28] into the proposed system, allowing for the tracking of circular obstacles. The

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**Algorithm 2:** Determine the convexity or concavity of the point-cloud block

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**Data:**

$o_i \leftarrow$  The origin of the lidar;

$T_{io} \leftarrow$  The threshold;

$N \leftarrow$  The number of measurement points in the point-cloud block

$B \triangleq \{p_i\}, i \in [1, N]$ ;

$V_i \leftarrow$  the vector storing  $N_i$  points inside  $\Delta o_i p_1 p_N$ ;

$V_o \leftarrow$  the vector storing  $N_o$  points outside  $\Delta o_i p_1 p_N$ ;

$r_{io} \leftarrow$  the ratio of the numbers of points inside  $\Delta o_i p_1 p_N$  to outside  $\Delta o_i p_1 p_N$ ;

Suppose that the order of three points consisting of the triangle  $\Delta o_i p_1 p_N$  is anticlockwise such as  $o_i, p_1, p_N$ .

True represents  $B$  is convex relative to the origin of the lidar;

False denotes  $B$  is concave relative to the origin of the lidar.

```

1 While (i ≠ N) do
2   Calculate three cross products as follows,
3    $T_1 = p_i o_i \otimes p_i p_1$ ;
4    $T_2 = p_i p_1 \otimes p_i p_N$ ;
5    $T_3 = p_i p_N \otimes p_i o_i$ ;
6   If ( $T_1 > 0 \ \&\& \ T_2 > 0 \ \&\& \ T_3 > 0$ )
       || ( $T_1 < 0 \ \&\& \ T_2 < 0 \ \&\& \ T_3 < 0$ )
7     Put  $p_i$  into  $V_i$ 
8   Else
9     Put  $p_i$  into  $V_o$ 
10  End
11   $r_{io} = \frac{N_i}{N_o}$ ;
12  If ( $r_{io} > T_{io}$ )
13    True;
14  End
15  False.
```

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**Output:** True or False

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detailed tracking algorithm is described in this section. Specifically, we introduce how any dynamic obstacles with any shape to be modeled such as to be tracked. In terms of tracking new dynamic obstacles, the state initialization is non-trivial due to the motion arbitrariness and independent of each other. New dynamic obstacles can be initialized by the system and put into new track containers while static obstacles need to be merged into the static background for achieving dynamic tracks. After initializing a new track, we put it into the set of existing dynamic tracks if it is continuously detected more than predefined times; otherwise, this track will be discarded.

### 1) Hierarchical data association

#### A) Coarse-level data association

After classing the measurements from a lidar scan, the point-cloud segment (point set) is then assigned to the static background or a dynamic obstacle recursively. The target of the data association is to figure out which detected obstacle taken at the last time interval  $t - 1$  corresponds to which detected obstacle captured at the current time interval  $t$  (Note that  $t - 1$  represents the last time interval rather than the time before 1 second). Specifically, to track obstacles, two-point sets  $P$  and  $Q$  detected at different time intervals are aligned. The global nearest-neighbor search algorithm is applied to finding the “best” fits for the existing tracks. If no correspondences are found for some point sets, then these point sets are considered as new tracks and are initiated by the Kalman filter. The new point set  $P$  is associated with its nearest neighbor  $Q$  if the Euler distances of their positions and radii are within two thresholds (5 and 3) respectively;

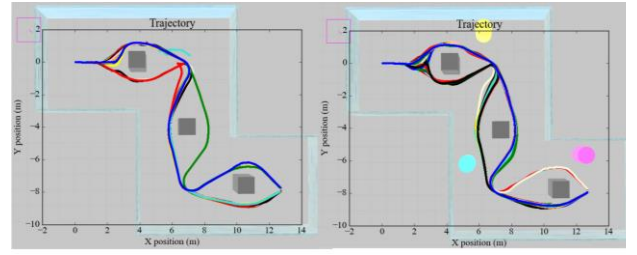


Figure 4. Simulation tests in the z-shape area with different placements of 3 (left side) and 6 (right side) obstacles, respectively.

otherwise, it is considered as a new point set to be tracked. First, obstacles detected at  $t - 1$  are considered as old obstacles, and obstacles detected at  $t$  are regarded as new obstacles. Then, we obtain the distances between each old obstacle and each new obstacle regarding the positions and the sizes by a traversing algorithm. Third, for each old/new obstacle, we ascendingly sort its distances with new/old obstacles. Thus, corresponding new/old obstacles with minimum distance to each old/new obstacle are extracted. Based on the pairing information, two preliminary correspondence maps including  $M_{n \rightarrow o}$  and  $M_{o \rightarrow n}$  are generated. Finally, a preset distance threshold  $T_{max}$  ( $T_{max} = 5$ ) is used in  $M_{n \rightarrow o}$  and  $M_{o \rightarrow n}$  for removing the correspondences with distances larger than  $T_{max}$ . We update these correspondences to the map  $M_r$ .

#### B) Fine-level data association

Given  $M_r$ , the fine level data association can further take into account the following correlations among observations. Normally, each detected new obstacle corresponds to only one old obstacle in the environment. However, in this resulted correspondence map, there might be that one new/old obstacle is associated with multiple old/new obstacles. A case example is human's legs while walking. These two cases can be detected by exploring the duplicate correspondences in the map  $M_r$ . Determination of the correspondence type for currently examined obstacles provides crucial information in terms of the state update. The state of a new obstacle is updated, relying on old obstacles. Any new obstacle is updated depending on the original obstacle in the second case. All obstacles involved in these two cases are marked as tracked ones.

It is possible that some new obstacles are not associated with any old obstacle after the data association. These unmatched point sets are then regarded as new obstacles in the proposed detection and tracking system. These new obstacles are put into the dynamic map such as to be initiated and tracked by KFs. If an obstacle is deemed dynamic, its state is estimated by KF.

### 2) Kalman filter

For realizing dynamic avoidance, the perception system needs to estimate the motion parameters of each moving obstacle. For tracking obstacles, we utilize Kalman filter[28] to estimate the states of detected obstacles. Each newly detected obstacle marked as tracked will be initialized by a separate filter. For each sample time, the used filter updates the prediction and the correction steps. The position and size of obstacles and the rates of change of each variable describing



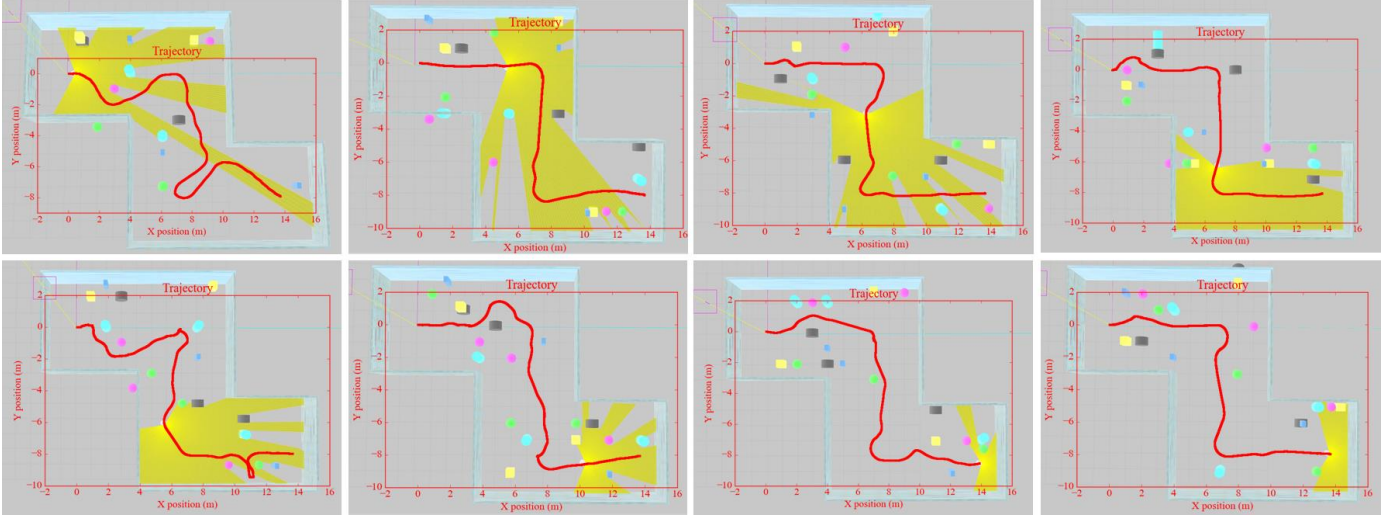


Figure 5. Eight different cases of robotic avoiding many obstacles spawned in random locations. The thick red curves represent the trajectories of the mobile robot avoiding obstacles deployed by the system randomly; spheres, cubes and cylinders with different colours denote obstacles; the yellow areas are detected by the robot's lidar.

the obstacle's state are estimated for realizing the safe navigation of a mobile robot in the 2D environment. We denote a vector including detected obstacles as  $\mathcal{A}_t$  at the time instant  $t$ . This vector is provided as follows:

$$\mathcal{A}_t = \{\mathcal{A}_t^i, i \in [1, n], n \geq 1\} \quad (6)$$

where

$$\mathcal{A}_t^i = [x_t^i, \dot{x}_t^i, y_t^i, \dot{y}_t^i, r_t^i, \dot{r}_t^i, I_t^i]^T$$

and  $n$  represents the number of obstacles in an environment. Eq. 6 illustrates the state of the  $i^{\text{th}}$  obstacle, with  $x_t^i$  and  $y_t^i$  being the position of the obstacle,  $r_t^i$  the circle radius,  $\dot{x}_t^i$  and  $\dot{y}_t^i$  the linear velocities, and  $I_t^i$  the index of the obstacle. Due to the invariance of the index of the obstacle, we omit the parameter in the equations. With such a definition of the state vector, we present the track state transition modeled:

$$\mathcal{A}_{t+1}^i = F\mathcal{A}_t^i + Gw_t \quad (7)$$

$F$  is expressed as follows:

$$F = \begin{bmatrix} A & 0 & 0 \\ 0 & A & 0 \\ 0 & 0 & A \end{bmatrix} \text{ with } A = \begin{bmatrix} 1 & s \\ 0 & 1 \end{bmatrix} \quad (8)$$

$s$  is the length of a sampling period.  $G$  represents the noise gain matrix, which is expressed as follows,

$$G = \begin{bmatrix} B & 0 & 0 \\ 0 & B & 0 \\ 0 & 0 & B \end{bmatrix} \text{ with } B = \begin{bmatrix} \frac{1}{2}s^2 \\ s \end{bmatrix} \quad (9)$$

The measurement equation can be formulated as follows:

$$m_{t+1} = H\mathcal{A}_{t+1}^i + v_{t+1} \quad (10)$$

where  $H$  is the measurement model, expressed as:

$$H = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \end{bmatrix} \quad (11)$$

According to the chosen kinematics model, the process noise  $w_t$  and measurement noise  $v_{t+1}$  satisfy zero-mean white Gaussian noise distributions

$$\begin{aligned} p(w) &\sim N(0, Q) \\ p(v) &\sim N(0, R) \end{aligned} \quad (12)$$

Thus, covariance kernels

$$E\{w_{t_i}w_{t_j}^T\} = Q_{t_i}\delta_{ij}$$

$$E\{v_{t_i}v_{t_j}^T\} = R_{t_i}\delta_{ij} \quad (13)$$

where  $\delta_{ij}$  is Kronecker delta function. When all of the parameters are known, the Kalman filtering equations are:

$$\hat{\mathcal{A}}_{(t|t)}^i = \hat{\mathcal{A}}_{(t|t-1)}^i + K_t[m_t - H\hat{\mathcal{A}}_{(t|t-1)}^i] \quad (14)$$

$$\hat{\mathcal{A}}_{(t+1|t)}^i = F\hat{\mathcal{A}}_{(t|t)}^i \quad (15)$$

where  $\hat{\mathcal{A}}_{(t|t)}^i$  is the estimate of  $\mathcal{A}_t^i$  based on the measurements  $\{m_0, \dots, m_t\}$  and  $\hat{\mathcal{A}}_{(t+1|t)}^i$  is the prediction of  $\mathcal{A}_{t+1}^i$  with the measurements  $\{m_0, \dots, m_t\}$ . The matrix  $K_t$  is the "Kalman filter gain" and is determined by

$$K_t = P_{(t|t-1)}H^T[HP_{(t|t-1)}H^T + R_t]^{-1} \quad (16)$$

where the covariance matrix of the error in predicting  $\mathcal{A}_t^i$  is provided as

$$P_{(t|t-1)} = E\{[\mathcal{A}_t^i - \hat{\mathcal{A}}_{(t|t-1)}^i][\mathcal{A}_t^i - \hat{\mathcal{A}}_{(t|t-1)}^i]^T\} \quad (17)$$

and  $P_{(t|t-1)}$  is computed using

$$P_{(t+1|t)} = FP_{(t|t)}F^T + GQG^T \quad (18)$$

where

$$P_{(t|t)} = P_{(t|t-1)} - K_tHP_{(t|t-1)} \quad (19)$$

Generally, one new tracked obstacle corresponds to just one old obstacle. If a new obstacle maps more than one old obstacles, we use the average of states of old obstacles to be that of the new obstacle. When an old obstacle has more than one corresponding new obstacles, the original obstacle is copied for each new detected one, and their states are updated in new information sets.

The convexity-concavity characteristics of the circle-shape model are invariant with respect to the distance. However, the size of the circle is adjusting with the measurement distance changing. Tracking the obstacle aims to achieve the state  $\mathcal{A}_k$  of the circle representing an obstacle in real time for realizing the avoidance. The state includes the position, the radius, the velocities, the changing rate of the radius and the obstacle identification(ID). All the parameters in the state are updated at the same time. Hence, in parallel with the assigned obstacle, the parameters of the circle are conveyed to the avoidance

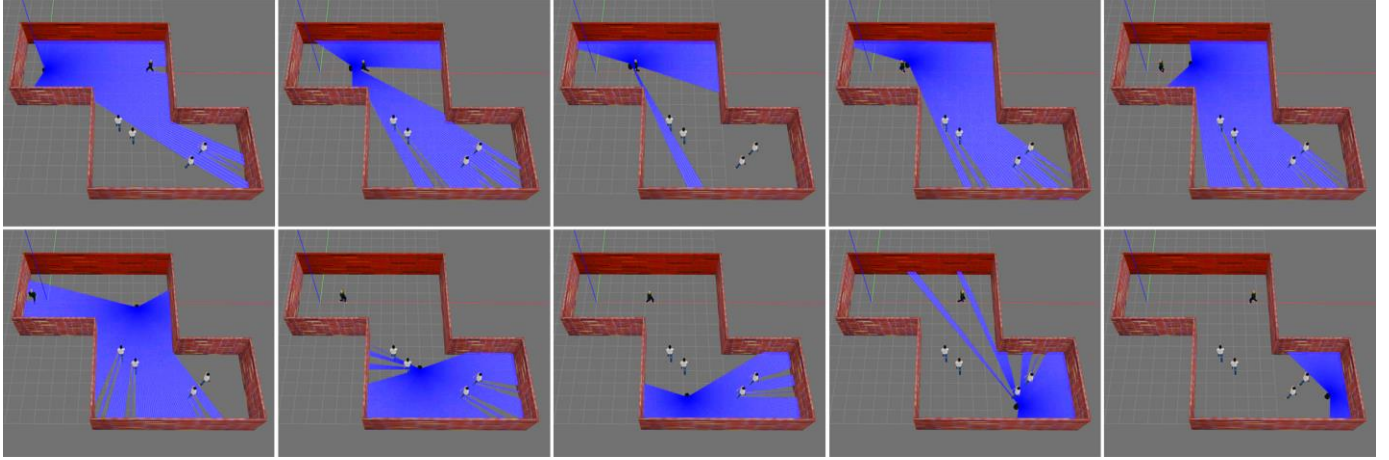


Figure 6. Snapshots of robotic avoiding the dynamic walking person and static persons.

system.

#### IV. EXPERIMENTS AND DISCUSSIONS

Here we evaluate the proposed avoidance strategy quantitatively and qualitatively. The performance of the proposed method is compared against one benchmarking obstacle avoidance approach that is a standard solution (TEB local planner + cost-map converter) in ROS in simulated scenarios (A); the case of robotic avoidance experiments in real-word environments (B).

The simulations and real experiments of avoiding obstacles are implemented on a Turtlebot-2 mobile robot with two wheels and a Hokuyo 2D laser scanner. The measurement distance is up to 20 meters and the sampling rate is 100 milliseconds and the angular resolution is  $0.36^\circ$  for the used laser scanner. Indeed, the thresholds  $T_d$ ,  $T_N$ , and  $T_{max}$  are determined experimentally according to the specific environment and the characteristic parameters of the 2D laser scanner. For instance, if the surrounding environment is small, we need to make  $T_{max}$  smaller.

##### A. Simulation Experiments

Simulation serves to create highly repeatable and consistent test conditions for evaluating a variety of avoidance implementations. To verify that the proposed algorithm is robust with dynamic layouts and obstacles, we conduct a lot of simulations with the open-source simulation platform-Gazebo. We locate obstacles along the path defined by 3 setting goals for (1) and 1 setting goal for (2). Before the simulation, we first run the SLAM algorithm [29] around the built environment to construct a global map. For every instantiated scene, we initialize the navigation pipeline with the detection-tracking algorithm and TEB local planner. The objective of each task for the robot is to simply move from the initial position to the destination without crashing.

###### 1) Avoiding new static and dynamic obstacles

(A)The first group of navigation tests is conducted in a simulated environment that involves positioning obstacles in a z-shape area. The robot's goal is to travel 22 meters along the z-shape. The number of obstacles spawned is set to 3 and 6. For each quantity of obstacles, 50 trails are created. The two

test environments are depicted in Fig.4, one sparsely-populated scene and one more densely-populated scene with more diverse obstacle categories. The trajectory visualizations show in detail that the robot completes the avoidances successfully without collisions. Figure 4 records the dynamic trajectories of the mobile robot when it is operating around many obstacles. The participants traverse these areas with similar topology during each navigation route almost.

(B)The practical relevance of the complex trials is to enable the navigation of avoiding obstacles in crowded environments, where new obstacles are unpredicted. There are 50 trial scenes with randomly spawned obstacles. To increase the difficulty of the scenario, we add more new obstacles in a fixed spawn zone on the original map than before, thereby increasing the density of the "obstacle forest". For each area (top, middle and bottom areas), we put 6 new obstacles randomly. Figure 5 shows some examples of a robot avoiding a variety of obstacles spawned randomly in the z-shape area. The proposed system can enable a robot to achieve 96% successful rate of avoiding obstacles in such complex scenarios.

(C)As shown in Fig.6, these simulations are intended to evaluate the system's ability to avoid the dynamic obstacle in complex environments. The robot confronts one dynamic obstacle in the form of one person stepping into the way of the robot and several new obstacles (standing persons) that do not belong to the known map in the course. This is important as any realistic scenario always contains some forms of dynamic obstacles. We set the velocities of the robot and the walking person as 0.75m/s and 0.5m/s respectively.

Most of the trajectories of the robot include moderate serrations since there are new obstacles on the pathways. We conduct 50 simulations. The robot reaches the destination successfully and correctly responds to the turns and new dynamic or static obstacles, except 3 cases that the robot stops before the walking person and has collisions with the walking person.

Here we present an experimental case. For instance, a series of snapshots in Fig.6 shows the robot involved in this simulation can realize the dynamic avoiding obstacles via the proposed avoidance algorithm. The robot bypasses the walking person safely and also avoids several standing persons successfully on the robot.

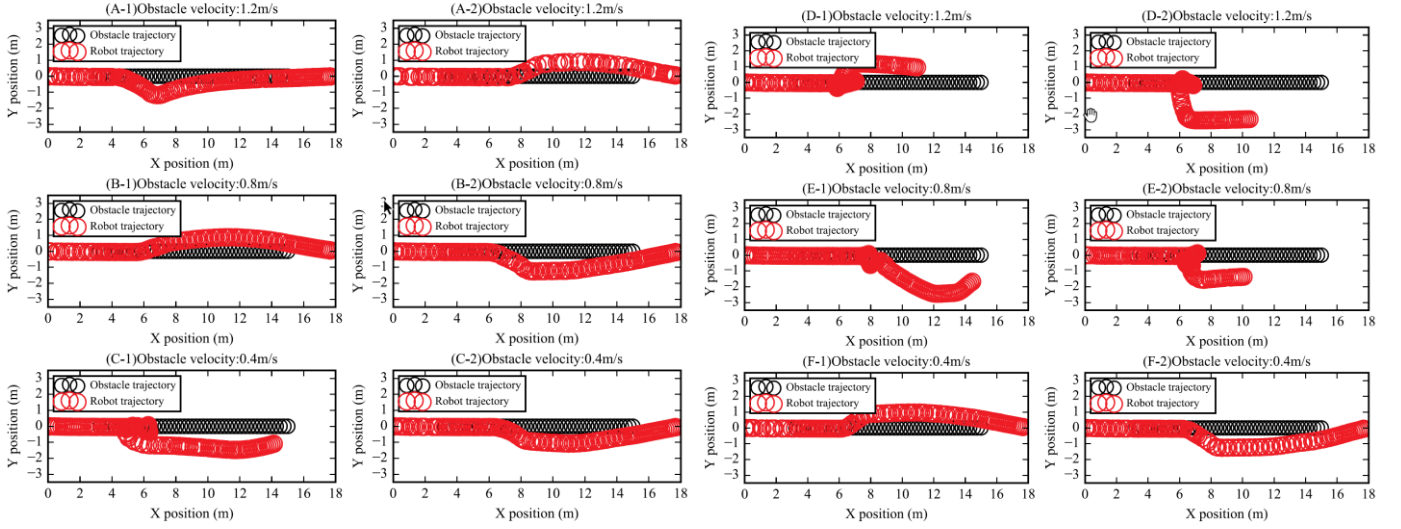


Figure. 7. The motion trajectories with the proposed approach(A,B,C) and the standard method (D,E,F). The velocity of the robot is 0.7m/s while the moving obstacle velocity has three values 0.4, 0.8 and 1.2m/s.

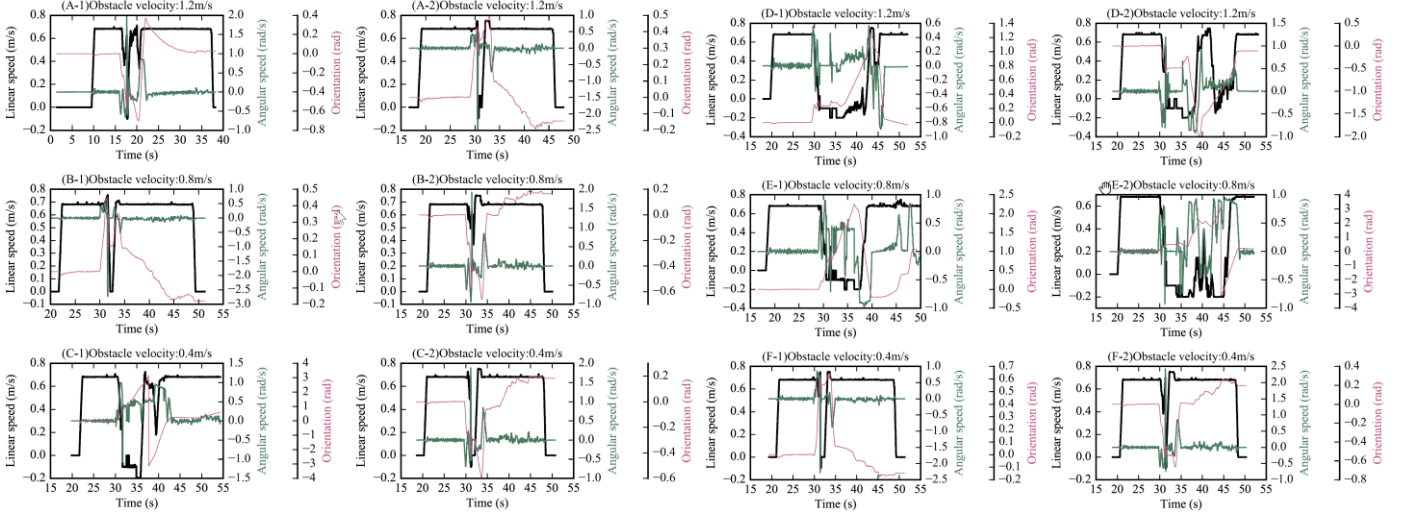


Figure. 8. The linear, angular speeds and the orientations with the proposed approach(A,B,C) and the standard method(D,E,F) for the cases of Fig. 7.

## 2) Performance comparison against the baseline system in dynamic scenarios

Figure 7 illustrates several simulation scenarios where a mobile robot needs to avoid a moving obstacle and attempts to arrive at the destination by a baseline avoidance strategy (TEB local planner + cost-map converter) in Fig.7(D-E-F) and the proposed strategy (TEB local planner + detection-tracking algorithm) with different obstacle's speeds from 0.4m/s to 1.2m/s with the 0.1m/s interval in Fig.7(A-B-C). Initially, the obstacle locates on the right side and the mobile robot stands at the left side in the simulation. Additionally, the goal is set at the right side of the obstacle so that the obstacle is located between the initial and final positions of the robot. Then, the moving obstacle moves towards the left direction while the robot moves toward the goal. Sequentially as it approaches the obstacle, the avoidance performance is executed. We evaluate the results with cases where the avoidance is successful by allowing the robot to execute its motion to the destination within the setting time(30s). In simulation environments, if the robot has a collision with the obstacle, the execution time will

be beyond the defined time. We declare failure if the robot does not arrive at the destination or use more than the setting time to complete. For each method with each speed of the obstacle, we simulate 200-time experiments of dynamic avoidances.

The avoidance process is clearly illustrated in Fig.7. The circles represent the footages of both the mobile robot and the moving obstacle respectively at the constant interval 0.2s in this figure. The distance of the centers of two successive circles indicates the velocity scale. That is, if this distance is big, the velocity is big, vice versa. From Fig.7, we can see that the velocity of the mobile robot decreases significantly when it avoids the heading obstacle. It can be seen that the trajectories of Fig.7(A-B-C) are smoother than the cases of Fig.7(D-E-F) in terms of the same velocity.

As for the cases of Fig.7(A-B-C), their linear, angular velocities and orientations are shown in Fig.8(A-B-C) for the proposed avoidance system respectively. Similarity, Fig. 8(D-E-F) also shows the linear, angular velocities and orientations of the cases of Fig.7(D-E-F). Although the linear velocity has



drastic impulses during the avoiding period, the motion remains almost smooth for the proposed avoidance system. With the linear speed of the obstacle increasing, the velocity of the mobile robot generally maintains the original value for the successful avoidances. It indicates that the proposed method is robust with the speed of the obstacle lower than 1.2m/s. Moreover, the angular velocity for the successful case is relatively smooth. In Fig.7(C-1, D-1, D-2, E-1, E-2), the robot and the obstacle have some collisions when they meet each other. The curves as shown in Fig. 8(A-B-C) have few sharp points at all the time. However, the curves as shown in Fig. 8(D-E-F) have a lot of sharp points. In terms of robot's orientations, the robot performs many turning actions if the robot and the obstacle have a collision.

The results of two systems are generated by varying the speed of the moving obstacle from 0.4m/s to 1.2 m/s. The proposed avoidance strategy realizes 91.12% successful rate of avoiding obstacles. The proposed method outperforms the baseline system by a significant margin (40.5%). This is somewhat expected since the baseline avoidance method always cost much computational resource to recognize the obstacles and is not working in real time. The proposed method allocates each track's frame of reference to be attached rigidly to the obstacle. Dynamic obstacles are approximated to cylinders and handled differently to static ones. As a result, as for the dynamic avoidance, the effectiveness of the proposed method is better than that of the baseline avoiding strategy in ROS. This illustrates that the proposed avoidance strategy works very well in such environments.

### B. Real Experiments

Lastly, we implement the proposed avoidance system on a mobile robot called Turtlebot-2 equipped with a 2D laser scanner. Given a goal and a known starting position, the robot tends to navigate through obstacles. A chair pushed by a person is moving forward as one dynamic obstacle. Figure 9 mainly shows the spatial evolution of detected and tracked obstacles in the human-robot involved scenario over a period of time. The robot first moves along the global path and only detects static obstacles. After a few seconds, a chair pushed by a person appears in the view of 2D lidar and is heading to the robot. The tracking algorithm based on KF reasonably estimates the obstacle's state by the iterations with measurements. The person continues moving towards the robot at around 0.5 m/s. The robot changes its direction to another side and then, passes through this chair successfully.

### C. Discussions

The baseline (TEB local planner + cost-map converter) which does directly represent obstacles as geometric primitives including points, lines, polygons is widely used for robotic navigation. However, once a large number of geometric primitives are involved, the baseline algorithm is generally considerably higher computational demand since huge parameters need to be addressed. Allowing for the limited computation power and real-time requirement, such a strategy is not available to handle fast-evolving scenarios where a mobile robot and moving obstacles "co-exist". In contrast, the proposed approach can realize a better avoidance



Figure. 9. Snapshots of dynamic avoidance.

performance. The proposed method processes the laser-point cloud for obtaining line segments and circles as consistent and meaningful representations of detected obstacles, which enormously reduces the computational resource. The corresponding reasons are twofold. First, in the geometric complexity, the lines and circles used for modeling the detected obstacles are just represented by four parameters and three parameters respectively. However, the compared baseline usually considers a polygon with at least six parameters as an obstacle. Second, in terms of quantitative terms of geometric primitives, a line segment with two points and a circle with one three parameters replace a lot of points, polygons to represent obstacles. Moreover, the laser scan is first processed with the segmenting, merging and classification algorithm described above, which significantly reduces the parameters to be solved. The proposed hierarchical data association integrated with an independent KF can improve the obstacle tracking accuracy by greedily assigning each observed geometric model. Integrating TEB local planner into the proposed detection-tracking algorithm, we enable the robot to realize dynamic avoidances. However, there is a challenge for the proposed avoidance perception strategy in understanding critical semantic information from a sliced sample of the world captured by a 2D scanner.

The dynamic avoidance is very complicated. The good dynamic avoidance system does not only require a robust perception system based on visual or laser sensors, but also needs suitable robotic control, localization, local and global path planners. Thus, a robustly dynamic avoidance requires all the sub-systems have good performances.

To evaluate the dynamic avoidance performance of the proposed strategy, we set relatively simple real experiments in cluttered real environments. Indeed, in practical scenarios, the dynamic avoidance strategy costs much computational

resource and thus, the performance is also limited by the computing power of a personal computer(PC), especially in cluttered surrounding environments. To solve this issue, we use a local PC to process the algorithm and send the commands to the robot by wireless; however, with a long distance between the local PC and the robot, the communication leads to a delay as well. It is well known that ROS structure cannot be in real time, which causes that we have to use a highly efficient perception system to relieve the communication delay in the ROS structure.

Moreover, there are two potentially complex dynamic avoidance experiments. In particular, a person walks through the line of the robotic heading direction, most cases are that the robot suddenly stops and then, continues moving without changing the direction after the person goes away. If the person stops before the robot, the robot stops and then, turns to continue moving. But actually, these two examples cannot show the performance of dynamic avoidance because generally, the robot does not need to configure the dynamic avoidance strategy and still can stop before an obstacle and update to a new trajectory. The spirits behind the set experiment with both a person and a robot face-to-face walking in the same line are twofold. First, if the robot cannot precisely track the dynamic person to obtain the position using the proposed perception algorithm, the robot would stop or have a collision with the person. Equipped with the proposed dynamic avoidance strategy, the robot keeps moving to the target point while tracking by updating the paths in real time. Second, due to face-to-face moving in the same line, the robot must turn a more angle to avoid the dynamic person. Otherwise, the robot just needs to rotate a small angle to avoid the obstacle when they are in different lines, in this case, it cannot illustrate an obvious avoidance performance.

## V. CONCLUSION

In this paper, we presented a novel avoiding strategy combined with the TEB local planner for realizing dynamic obstacle avoidance. We performed the simulations and real experiments to demonstrate the capabilities of the proposed avoidance system on the detection and tracking of obstacles in real time. Also, these experiments illustrated that the proposed system is robust and responsive to clutter environments. In the future, we will combine the 3D perception solution to recognize the obstacles represented directly by full 3D models to improve the capability of the robot navigation.

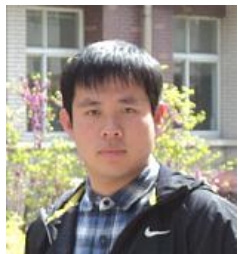
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